

1-2020

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### Recommended Citation

Kumar Singh, Vipin; Mihalkovic, Marek; Krajci, Marian; Sarkar, Shuvam; Sadhukhan, Pampa; Maniraj, M.; Rai, Abhishek; Pussi, Katariina; Schlagel, Deborah L.; Lograsso, Thomas A.; Kumar Shukla, Ajay; and Barman, Sudipta Roy, "Quasiperiodic ordering in thick Sn layer on i-Al-Pd-Mn: A possible quasicrystalline clathrate" (2020). *Ames Laboratory Accepted Manuscripts*. 587.

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# Quasiperiodic ordering in thick Sn layer on i-Al-Pd-Mn: A possible quasicrystalline clathrate

## Abstract

Realization of an elemental solid-state quasicrystal has remained a distant dream so far in spite of extensive work in this direction for almost two decades. In the present work, we report the discovery of quasiperiodic ordering in a thick layer of elemental Sn grown on icosahedral (i)-Al-Pd-Mn. The scanning tunneling microscopy (STM) images and the low-energy electron diffraction patterns of the Sn layer show specific structural signatures that portray quasiperiodicity but are distinct from the substrate.

Photoemission spectroscopy reveals the existence of the pseudogap around the Fermi energy up to the maximal Sn thickness. The structure of the Sn layer is modeled as a form of quasicrystalline clathrate on the basis of multiple supporting evidences: First, from *ab initio* total energy evaluation, the energy of bulk Sn clathrate quasicrystal is lower than the high-temperature metallic  $\beta$ -Sn phase, but higher than the low-temperature  $\alpha$ -Sn phase. A comparative study of the free slab energetics shows that surface energy favors clathrate over  $\alpha$ -Sn up to about 4-nm layer thickness and matches  $\beta$ -Sn for narrow window of slab thickness of 2–3 nm. Second, the bulk clathrate exhibits gap opening near Fermi energy, while the free slab form exhibits a pronounced pseudogap, which explains the pseudogap observed in photoemission. Third, the STM images exhibit good agreement with clathrate model. Finally, we establish the adlayer-substrate compatibility based on very similar (within 1%) the cage-cage separation in the Sn clathrate and the pseudo-Mackay cluster-cluster separation on the i-Al-Pd-Mn surface. Furthermore, the nucleation centers of the Sn adlayer on the substrate are identified and these are shown to be a valid part of the Sn clathrate structure. Thus, based on both experimental and *ab initio* density functional theory calculations, we propose that 4-nm-thick Sn adlayer deposited on fivefold surface of i-Al-Pd-Mn substrate is in fact a metastable realization of elemental, clathrate family quasicrystal.

## Disciplines

Engineering Physics | Materials Science and Engineering

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# Quasiperiodic ordering in thick Sn layer on *i*-Al-Pd-Mn: A possible quasicrystalline clathrate

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(Received 21 July 2019; published 8 January 2020)

Realization of an elemental solid-state quasicrystal has remained a distant dream so far in spite of extensive work in this direction for almost two decades. In the present work, we report the discovery of quasiperiodic ordering in a thick layer of elemental Sn grown on icosahedral (*i*)-Al-Pd-Mn. The scanning tunneling microscopy (STM) images and the low-energy electron diffraction patterns of the Sn layer show specific structural signatures that portray quasiperiodicity but are distinct from the substrate. Photoemission spectroscopy reveals the existence of the pseudogap around the Fermi energy up to the maximal Sn thickness. The structure of the Sn layer is modeled as a form of quasicrystalline clathrate on the basis of multiple supporting evidences: First, from *ab initio* total energy evaluation, the energy of bulk Sn clathrate quasicrystal is lower than the high-temperature metallic  $\beta$ -Sn phase, but higher than the low-temperature  $\alpha$ -Sn phase. A comparative study of the free slab energetics shows that surface energy favors clathrate over  $\alpha$ -Sn up to about 4-nm layer thickness and matches  $\beta$ -Sn for narrow window of slab thickness of 2–3 nm. Second, the bulk clathrate exhibits gap opening near Fermi energy, while the free slab form exhibits a pronounced pseudogap, which explains the pseudogap observed in photoemission. Third, the STM images exhibit good agreement with clathrate model. Finally, we establish the adlayer-substrate compatibility based on very similar (within 1%) the cage-cage separation in the Sn clathrate and the pseudo-Mackay cluster-cluster separation on the *i*-Al-Pd-Mn surface. Furthermore, the nucleation centers of the Sn adlayer on the substrate are identified and these are shown to be a valid part of the Sn clathrate structure. Thus, based on both experimental and *ab initio* density functional theory calculations, we propose that 4-nm-thick Sn adlayer deposited on fivefold surface of *i*-Al-Pd-Mn substrate is in fact a metastable realization of elemental, clathrate family quasicrystal.

DOI: [10.1103/PhysRevResearch.2.013023](https://doi.org/10.1103/PhysRevResearch.2.013023)

## I. INTRODUCTION

The mathematical concept of aperiodic ordering and the discovery of quasicrystals brought paradigm shift in crystallography [1,2]. Quasiperiodicity has been observed in naturally occurring minerals [3], different intermetallic compounds [4], binary nanoparticle superlattices [5], colloidal quasicrystals [6], oxide thin films [7], and large molecular assemblies [8,9]. A recent exciting finding is the nontrivial topological property of quasiperiodic systems [10,11]. The technological importance of quasicrystals arise from their low frictional coefficient, heat insulation, and photonic band gap [12,13].

However, the chemical complexity of quasicrystals discovered so far hinders their applicability and basic understanding of their unusual properties. An elemental quasicrystal would be best suited for this purpose, but a single-element bulk quasicrystal has not been yet observed. Efforts in this direction for over a decade have involved the use of quasicrystalline substrates as a template to grow quasiperiodic elemental layers [14–26]. Pseudomorphic growth of one monolayer (ML) quasiperiodic Sn has been reported in the past on decagonal (*d*)-Al-Ni-Co [15] and icosahedral (*i*)-Al-Cu-Fe [16]. A density functional theory (DFT) study predicted pseudomorphic growth of quasiperiodic Sn on *i*-Al-Pd-Mn [17]. In most of the studies in the past, only the first wetting layer has been reported to exhibit fivefold quasiperiodicity with a structure similar to the substrate. Pb/*i*-Ag-In-Yb showed fivefold growth isostructural with the substrate, and pentagonal motifs with maximum height of about 0.7 nm were identified [25]. It may be noted that although the thickness was substantial, fivefold quasiperiodicity was not observed in 25 ML Cu/*i*-Al-Pd-Mn [27] or in 1.8-nm-thick Ag on GaAs [28]; rather, aperiodic modulation of row separation were observed only in one direction.

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It is interesting to note that elements from group XIV of the periodic table have specific propensity to form pentagonal or even icosahedral structures. Although Sn exhibits a diamond-type structure ( $\alpha$ -Sn, space group  $Fd\bar{3}m$ ) at low temperature and a tetragonal structure ( $\beta$ -Sn, space group  $I4_1/amd$ ) above 286 K, it is well known that Sn can form  $sp^3$ -bonded *clathrate* structures whose canonical constituents are four kinds of cages that are bounded exclusively by pentagonal and hexagonal faces. Out of the four canonical cages, the most abundant one in common clathrate crystals is the dodecahedral cage with icosahedral symmetry, bounded exclusively by 20 pentagonal faces, in contrast to purely hexagonal diamond structure (see Fig. 5 in Sec. III D). Intriguingly, in their computer simulation, Engel *et al.* [29] observed spontaneous formation of three icosahedral phases, and the “loosely packed” phase can be regarded as an imperfect realization of the icosahedral quasicrystal clathrate. Last but not the least, the dodecahedron cage found in clathrates is identical with the second shell of the so-called mini-Bergman clusters, playing a fundamental role in *i*-Al-Pd-Mn structure.

In this work, we observed that Sn deposited on *i*-Al-Pd-Mn surface retains quasiperiodic ordering up to maximal achievable coverage leading to nearly 4 nm thickness, indicating the existence of the first intrinsic—although apparently metastable—monoatomic realization of a quasicrystal. We model it as a quasicrystal structure belonging to the clathrate family strictly maintaining tetrahedral coordination consistent with  $sp^3$  bonding. We justify plausibility of the model by energetic considerations within the DFT framework, based on the structural comparison with experimentally observed motifs and from the character of electronic density of states (DOS) near Fermi energy.

## II. METHODS

The single-grain fivefold *i*-Al-Pd-Mn quasicrystal surface was prepared by repeated cycles of  $Ar^+$  ions sputtering and annealing to about 900–930 K for 2–2.5 h. The cycles were repeated until a sharp fivefold low energy electron diffraction (LEED) pattern was observed. Sn (99.99% purity) was evaporated from a water-cooled Knudsen evaporation cell [30]. The evaporation cell was operated in the temperature range of 1073–1163 K at a pressure of  $2 \times 10^{-10}$  mbar during the deposition. For the thick layer growth, we used an effective deposition rate of 0.06 to 0.4 ML/min in repeated cycles of 1 min of deposition followed by 1 min of waiting time. Sn deposition was carried out with the substrate close to room temperature (RT  $\sim$  300–330 K) and at 150 K. The temperature of the substrate was measured using a K-type thermocouple.

The STM measurements were carried out at a base pressure of  $2 \times 10^{-11}$  mbar using a variable temperature STM from Omicron GmbH. STM measurements were performed at RT and 80 K in the constant current mode using a tungsten tip that was cleaned by field emission, sputtering, and voltage pulse method. The tip was biased and the sample was kept at the ground potential. It may be noted that same kind of tiles and motifs are observed for different bias voltages ranging from  $-2.6$  to  $2.8$  V for different coverages, which demonstrate that the features are topography related. The zero in the vertical scale of a STM image is set at the bearing height, which is the

most dominant height value, based on a height distribution histogram. LEED was performed using four-grid rear view optics from OCI Vacuum Microengineering.

The ultraviolet photoemission spectroscopy (UPS) measurements at 150 K were performed using R4000 electron energy analyzer with wide-angle lens using 21.2-eV photon energy incident at  $45^\circ$  with respect to (wrt) the surface normal and measured in normal emission, with an analyzer acceptance angle of  $\pm 15^\circ$  in transmission mode and a resolution of 50 meV. The Fermi edge was measured on a metallic sample in electrical contact with the specimen. X-ray photoelectron spectroscopy (XPS) measurements were performed with 1253.6 eV ( $MgK\alpha$ ) photon energy with a resolution of 0.8 eV using Phoibos 100 electron energy analyzer. The thickness of the Sn adlayer has been determined by STM and also by XPS from the intensities of Sn 3d and Al 2p core level peaks using the well-known relations  $I_{Sn3d} = I_{Sn3d\infty}[1 - \exp(-d/\lambda \cos \theta)]$  and  $I_{Al2p} = I_{Al2p\infty} \exp(-d/\lambda \cos \theta)$ , where  $d$  is the thickness,  $\theta$  is the emission angle ( $55^\circ$ ), and  $\lambda$  is the mean free path.  $\lambda$  for Sn 3d (14.2 Å) and Al 2p (19.6 Å) are consistent with Ref. [31].

The DFT calculations have been carried out using the Vienna *ab initio* Simulation Package (VASP) [32] by performing an iterative solution of the Kohn-Sham equations of DFT within a plane-wave basis. We use projector augmented wave potentials [33] in the PW91 generalized gradient approximation [34]. For both bulk and free slab structures, the cohesive energies are converged to less than 1 meV/atom with basis set containing plane waves with a kinetic energy up to  $E_{\text{cutoff}} = 150$  eV. The self-consistency iteration were stopped when total energies are converged to within  $10^{-6}$  eV. All the structures, bulk models as well as slabs, were fully relaxed without constraints, including the cell parameters.  $k$ -point meshes have been converged to satisfy for each mesh dimension  $\alpha$   $N_{k\alpha} \times c_\alpha \sim 100$ , where  $c_\alpha$  are edges of the periodic cell.

## III. RESULTS AND DISCUSSION

### A. STM and LEED of monolayer Sn on *i*-Al-Pd-Mn

We begin our discussion with a high-resolution STM image of 1 ML Sn/*i*-Al-Pd-Mn in Fig. 1(a). It is clearly quasiperiodic, as demonstrated by its Fourier transform (FT) that exhibits two sets of spots of tenfold symmetry highlighted by yellow circles [Fig. 1(b)], whose distance from the center (white lines) is in the ratio of  $\tau$ , where  $\tau$  is the golden mean ( $\approx 1.618$ ). The most prevalent tile in the Sn layer is a pentagon with a central dark region [Fig. 1(c)], as shown by black dashed lines. The length of the sides of these pentagonal ( $P$ ) tiles is around 0.7 nm, as shown by its length distribution in Fig. S1(a) of the Supplementary Material (SM) [35]. Hexagonal tiles, although rare, are also observed with length scale similar to the  $P$  tiles [Fig. 1(d)]. The different motifs formed by the congregation of such tiles are highlighted by circles in Fig. 1(a). A distinctive motif of the Sn layer that is not observed for *i*-Al-Pd-Mn is a circular congregation having common sides that we refer to as wheel motif (yellow dashed circles), while half-circular or incomplete wheel motif is named as crown motif (white



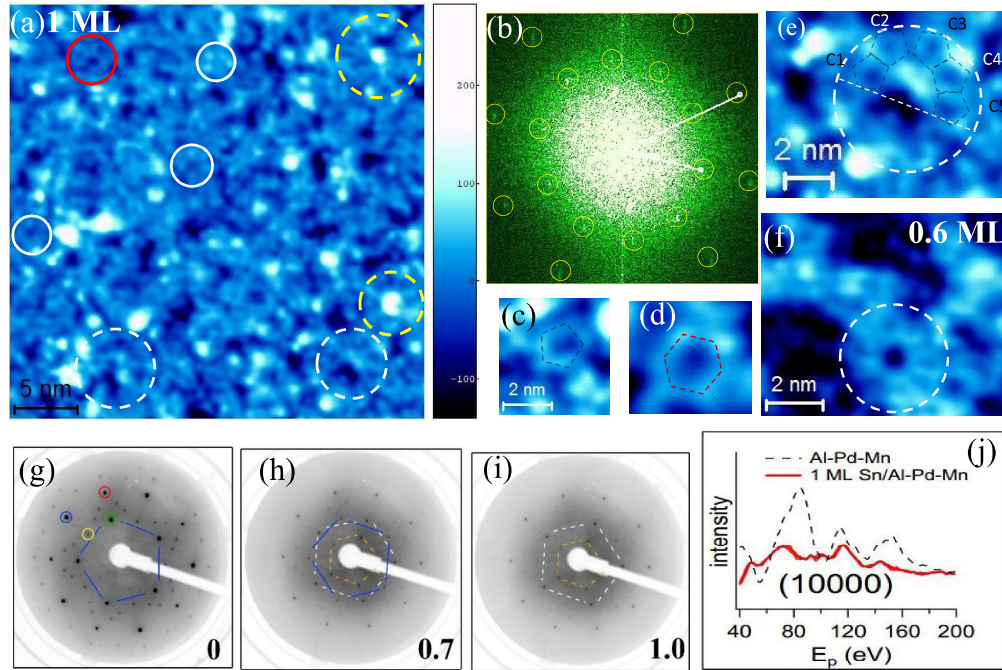


FIG. 1. (a) High-resolution STM topography image with tunneling current ( $I_T = 0.2$  nA) and bias voltage ( $U_T = 1.5$  V) for 1 ML Sn/*i*-Al-Pd-Mn at room temperature (RT); various motifs are marked by circles. The color scale with the height in picometers is shown on the right, where zero corresponds to the bearing height. (b) Fourier transform (FT) of the STM image of 1 ML Sn/*i*-Al-Pd-Mn; the spots are highlighted by yellow circles. The (c) pentagonal (*P*) and (d) hexagonal tiles are shown in expanded scale. (e) The crown motif enclosed by a white dashed circle formed by *P* tiles marked C1 through C5 (dashed black lines). (f) 0.6 ML Sn/*i*-Al-Pd-Mn with  $I_T = 0.6$  nA,  $U_T = 2.8$  V. The STM images are shown after low-pass FT filtering. LEED patterns at beam energy of 81 eV for (g) *i*-Al-Pd-Mn (h) 0.7 ML Sn/*i*-Al-Pd-Mn, and (i) 1 ML Sn/*i*-Al-Pd-Mn in inverted scale; coverage is indicated in ML at the bottom right corner. (10000), (000 $\bar{1}0$ ), (00 $\bar{1}\bar{1}0$ ), and (11000) LEED spots are highlighted by green, yellow, red, and blue circles, respectively, in panel (g). (j) Experimental IV curve for (10000) spot of 1 ML Sn/*i*-Al-Pd-Mn compared to that of *i*-Al-Pd-Mn.

dashed circle). An expanded view of a crown motif, seen in the bottom right corner of Fig. 1(a), is shown in Fig. 1(e). It shows five *P* tiles (C1 to C5) clearly not in the same plane forming a half circle. Noteworthy is that the height profiles (Fig. S1(b) of SM [35]) along the sides of these tiles show the maximum puckering to be about 0.06 nm, which is sizable compared to the thickness of the first layer (0.26 nm). The puckered nature of the Sn layer can also be quantified by the root-mean-square roughness ( $S_q$ ), which turns out to be 0.04 nm, which is twice that of *i*-Al-Pd-Mn ( $S_q = 0.02$  nm). A hexagonal tile centered motif in red circle in the top left side of Fig. 1(a) also indicates that the tiles are not in the same plane. It is noteworthy that even in the submonolayer regime, for example, at 0.6 ML, as the Sn adatoms form islands, the crown motif is observed [white dashed circle in Fig. 1(f)]. In contrast to the *P* tiles that are uniform, pentagons with bright vertices with side length of about 1.1 nm are occasionally observed [white circles in Fig. 1(a)]. These are different from the white flowers of *i*-Al-Pd-Mn because here a central dark region is observed.

The LEED of the Sn monolayer is distinctly different from the substrate: The latter recorded with beam energy ( $E_p$ ) of 81 eV exhibits two sets of 10 spots, inner and outer [Fig. 1(g)], in agreement with literature [36,37]. A blue pentagon connects the intense (10000) spots of the inner set, while (00 $\bar{1}\bar{1}0$ ) and (11000) spots on the outer set are also indicated by circles. As Sn coverage increases, the intensities of (000 $\bar{1}0$ )

spots increase (white dashed pentagon), whereas in contrast the (10000) intensities decrease (blue pentagon) [Fig. 1(h)]. Furthermore, a set of five innermost spots appears forming a smaller pentagon (yellow dashed) with an orientation rotated 36° wrt the blue pentagon. In the LEED pattern for 1 ML Sn in Fig. 1(i), the spots joined by white and yellow dashed pentagons remain clearly visible, while the (10000) spots become inconspicuous. At other  $E_p$  too, the LEED pattern is modified (Fig. S2 of SM [35]). Consequently, the intensity versus beam energy (IV) curves for (10000) in Fig. 1(j) [as well as for (000 $\bar{1}0$ ), (00 $\bar{1}\bar{1}0$ ) and (11000) spots in Fig. S3 of SM [35]] are different between the Sn monolayer and *i*-Al-Pd-Mn, demonstrating the structural differences between the two.

## B. STM and LEED of Sn multilayers

The growth of the second layer is initiated by formation of condensed islands, as shown in the STM image for 1.4 ML Sn/*i*-Al-Pd-Mn [Fig. 2(a)]. The height distribution histogram [inset, Fig. 2(a)] and the height profiles given in Fig. 2(b) along *ab* and *cd* in an extended area image in Fig. S4 [35] show that all the islands representing the second layer are  $\approx 0.2$  nm thick, indicating layered growth. This is expected [38] because the surface energy of Sn (0.71 J/m<sup>2</sup>) [39,40] is less than that of *i*-Al-Pd-Mn (0.82 J/m<sup>2</sup>) [41]. Figure 2(c) shows the fully formed second layer, and the motifs are highlighted by circles. The quasiperiodicity is confirmed by

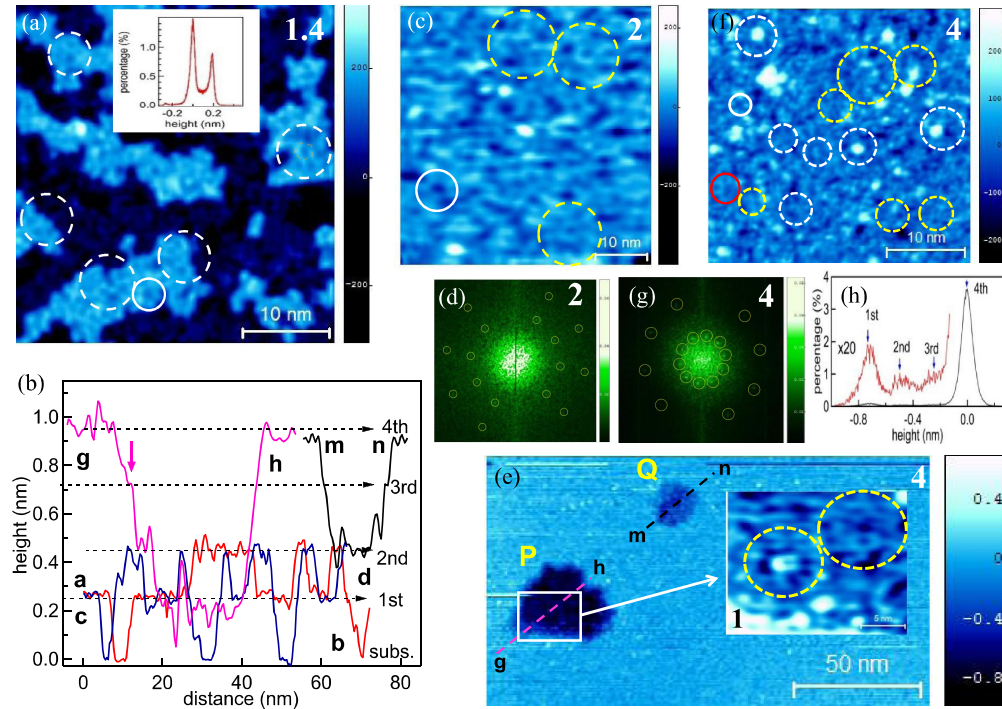


FIG. 2. (a) High-resolution STM topography image of 1.4 ML Sn/*i*-Al-Pd-Mn with  $I_T = 0.6$  nA and  $U_T = -2.6$  V at RT showing motifs that are encircled, the height distribution histogram in the inset shows two peaks corresponding to the first and the second Sn layer. (b) Height profiles along different directions as indicated in text. (c) STM topography image of the second Sn layer at RT, showing different motifs enclosed in dashed (yellow) and solid (white) circles. Coverage in ML is shown in the right-hand top corner of all the images. (d) Fourier transform of panel (c) corresponding to the second layer; the spots are highlighted by yellow circles. (e) STM topography image ( $I_T = 0.3$  nA,  $U_T = 2.5$  V) of the fourth Sn layer measured at RT after deposition at 150 K. The inset (white arrow) is the expanded part of the rectangle that shows the topography of the floor of the pit *P* to be similar to the Sn monolayer in Fig. 1. (f) High-resolution STM topography image ( $I_T = 0.2$  nA,  $U_T = 2.5$  V) of the fourth Sn layer showing different motifs enclosed in dashed and solid circles, and panel (g) shows the Fourier transform corresponding to the fourth layer. (h) Height histogram of the STM image in panel (e).

the FT [Fig. 2(d)] that shows two sets of spots (yellow circles) with tenfold symmetry, whose distance from the center is in ratio of  $\tau$ . The motifs are similar to the monolayer of Sn discussed in the previous section. The wheel (yellow dashed circle) and pentagon with bright vertices (white circle) are observed. The second layer is also puckered with  $S_q = 0.05$  nm.

In order to enhance the thickness, we have deposited Sn at a lower temperature (150 K) since it is very difficult to grow thicker layers at RT despite longer time deposition because of the low sticking rate of Sn. The occurrence of the fourth layer is established by analyzing the pit *P* in lower left corner of Fig. 2(e). The inset is the expanded image of the floor of *P* that is enclosed by the white rectangle. It shows Sn motifs similar to a Sn layer and hence it is at least 1 ML thick. Thus, the three weak peaks in the height distribution histogram [Fig. 2(h)] can be assigned to the first (floor of the pit *P*), second (floor of the pit *Q*), and third (at edges of pits *P* and *Q*) layers, while the main peak corresponds to the fourth layer. The height profiles along lines *gh* and *mn* in Fig. 2(b) also show this; the transition from third to fourth layer is shown by a change in slope (pink arrow). In fact, the pink height profile along *gh* shows formation of three Sn layers of nearly equal heights. This is incompatible with the quasiperiodic step heights of the *i*-Al-Pd-Mn substrate, hence confirming the growth of four Sn layers.

A high-resolution STM image for the fourth layer in Fig. 2(f) shows the wheel, crown (dashed circles), and the triplet motifs (red circle) that are similar to the thinner layers. FT corresponding to the fourth layer [Fig. 2(g)] exhibits two set of spots [Fig. 2(g)], whose distance from the center is in the ratio of  $1:\tau^2$ . The LEED patterns exhibit fivefold symmetry within the coherence length scale of the instrument (Fig. S5 [35]). It shows three sets of sharp spots comprising an inner set of nine spots forming a decagon (connected by yellow lines, the 10th spot is hidden by the shadow of the electron gun), four intermediate spots forming a pentagon (green dashed lines), and nine outer spots (dashed pink lines). Intensity profiles through each of the spots are also shown in Fig. S5. Quasiperiodicity is reasserted by the distances of the innermost, inner, and outer set of spots from (0, 0) in ratio  $1:1.63:2.7 \approx 1:\tau:\tau^2$ . Here, it is worth mentioning that in contrast to the present results, Sn grown on *i*-Al-Cu-Fe showed island growth after the first quasiperiodic layer [16] possibly because in that work the deposition was done at much higher temperatures (573–623 K) and large deposition rate of 15 ML/min, where activated diffusion of Sn across terraces might have resulted in clustering and island growth. In contrast, our deposition temperature for growing thicker layers is 150 K and the deposition rate is much lower (see Sec. II).



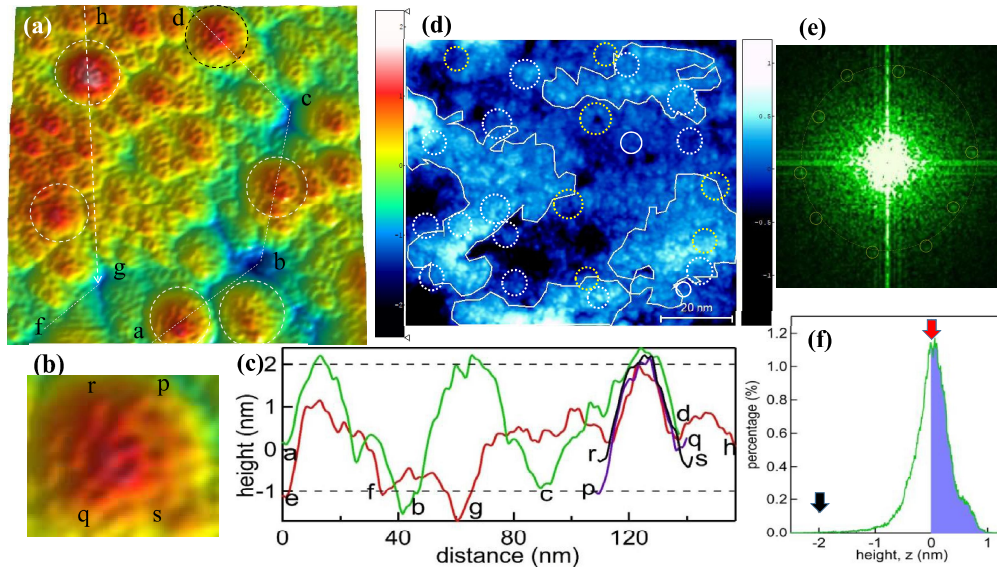


FIG. 3. (a) A  $104 \times 106$  nm STM topography image of quasiperiodic Sn showing three-dimensional growth using  $U_T = -1.5$  V,  $I_T = 0.5$  nA; measurement at 80 K after deposition at 150 K. (b) An expanded image of a dome enclosed by black dashed circle in A. (c) Height profiles along different directions of panels (a) and (b); see text. (d) STM topography image from a different region showing the motifs that are highlighted. The regions enclosed by white contour lines have thickness  $>3$  nm. (e) The FT of the image in panel (d) showing tenfold spots and (f) the height distribution histogram of panel (d).

### C. Thick Sn layer studied by STM and LEED

In order to obtain quasiperiodic Sn of even larger thickness, the deposition was done at 150 K for twice the time compared to the previous (fourth-layer) deposition and the layer was cooled down to 80 K. In this case, the STM image in Fig. 3(a) shows domelike structures of uniform shape with a circular base (highlighted by dashed circles). Interestingly, an expanded view of a dome in Fig. 3(b) shows a central pentagonal tile surrounded by other pentagonal tiles, forming a network. The maximum height of these domes is 3 nm from the base, as shown from the height profiles [Fig. 3(c)] along  $pq$  and  $rs$  of Fig. 3(b) and along  $abcd$  and  $efgh$  of Fig. 3(a). The diameter of the base of the domes exhibits a Gaussian distribution centered at 17.5 nm with a FWHM of about 10 nm, as shown in Fig. S6(a) [35]. The puckered nature of the surface is increased by a large amount as portrayed by  $S_q = 0.4$  nm.

However, possibly due to a competition between three-dimensional versus layered growth, the domes are not visible everywhere on the surface. For example, in Fig. 3(d), a different region shows relatively longer range undulations of  $\approx 50$  nm [see also Figs. S6(b) and S6(c) [35] for an extended area image and height profile]. It is relatively flat compared to Fig. 3(a) with smaller  $S_q = 0.3$  nm. Here, motifs such as wheel (yellow dashed circle), crown (white dashed circle), and pentagon with bright vertices (white circle) are observed. Moreover, in Fig. 3(e), the tenfold FT confirms the quasiperiodic nature of the layer; a marginal deviation in the arrangement of these spots from circle could be because of finite amount of thermal drift during scanning.

In order to find the thickness of this layer, we note that the peak of the height histogram at  $z = 0$  nm [red arrow in Fig. 3(f)] shows that about 50% of the area (shaded with blue

color) has a thickness (or height) of  $\geq 2$  nm wrt the minimum at  $z \approx -2$  nm (black arrow). The minimum region is identified to be around  $a$  in Fig. S6(b) from the height profile  $abc$  shown in Fig. S6(c). Since we obtain a thickness of 1 nm for the wetting layer, i.e., up to the fourth layer, an estimate of the thickness of the minimum region around  $a$  in Fig. S6(b) is  $\approx 1$  nm. Thus, the thickness of the regions enclosed by white contour lines in Fig. 3(d) is  $\geq 3$  nm. The presence of many quasiperiodic motifs (encircled) in this region that are similar to the motifs observed in the 2- to 3-nm-thick region outside the contour lines or those in Figs. 1 and 2 indicates similar quasiperiodic structure in the  $\geq 3$  nm region. An estimate of the height of the Sn domes in Fig. 3(a), by the same argument discussed above, is  $\geq 4$  nm, since these are at a height of 3 nm from the base [Fig. 3(c)], and the base can be taken to be  $\geq 1$  nm in thickness.

The appearance of domes and undulations [Figs. 3(a) and 3(d)] is indicative of transformation toward quasiperiodic ordering in the vertical direction, which could be expected as the Sn adlayer becomes thicker. The growth transforms from puckered but primarily two dimensional to quasiperiodic growth in all three directions similar to a bulk quasicrystal. We find that the thick film is not stable when warmed up to RT, as is evident from 40–50% decrease of the Sn Auger signal, which is possibly caused by the Sn atoms diffusing out to the sides of the substrate. Diffusion of Sn from the back of Al-Ni-Co substrate to the front with increasing temperature has been reported in literature [15].

Further evidence of quasiperiodicity in this thick layer in the macroscopic length scale is provided by the LEED patterns that show sharp fivefold spots [Figs. 4(a)–4(c)]. The intensity profiles of each of the spots are shown in Figs. 4(d)–4(g). At 87 eV [Fig. 4(b)], the outer 10 spots and the inner pentagon are observed and the ratio of their distance from the (0,0) specular spot is  $1 : 1.63 \approx 1 : \tau$ . At beam energies of 46

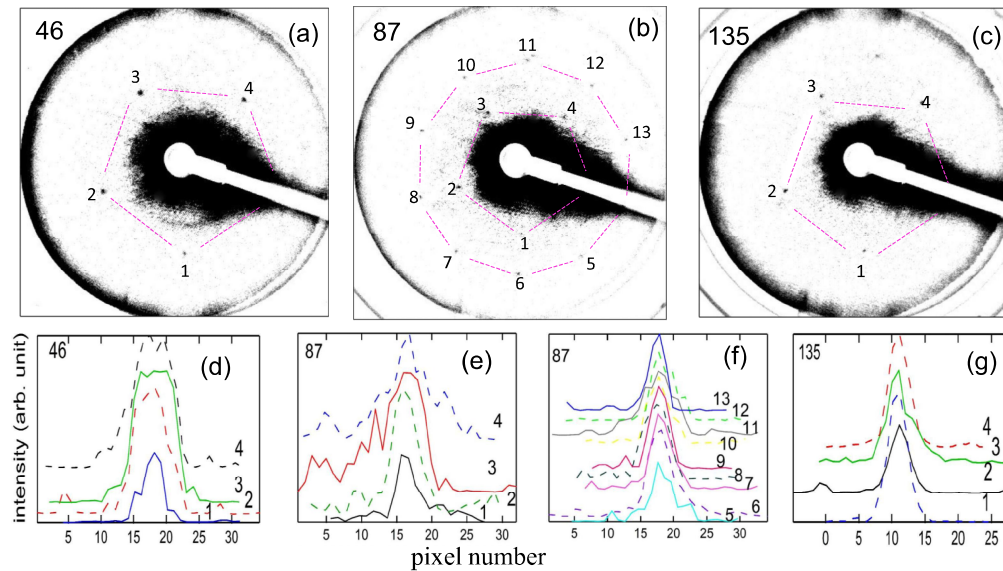


FIG. 4. LEED patterns of the 3- to 4-nm-thick Sn layer with beam energies (a) 46 eV, (b) 87 eV, and (c) 135 eV. The intensity profiles through the numbered spots (d) 1 through 4 for beam energy  $E_p = 46$  eV, [(e), (f)] 1 through 13 for  $E_p = 87$  eV, and (g) 1 through 4 for  $E_p = 135$  eV.

and 135 eV [Figs. 4(a) and 4(c)], four spots representing a pentagon are observed; the fifth spot is hidden by the shadow of the electron gun. In Fig. S7 [35], the IV curves for the thicker Sn layers are shown, and their peak positions are similar to those of 1 ML Sn, indicating their structural similarity. LEED patterns as a function of beam energy are shown by the video files in the SM, such as *3nmleed* for the 3-nm Sn layer, *1.8nmleed* for 1.8-nm Sn layer, *1nmleed* for 1-nm Sn layer, and *0.25nmleed* for the 0.25-nm (or 1 ML) Sn layer [35]. If an adlayer has different domains, it results in the appearance of multiple spots in the LEED pattern. There are reports of such rotational epitaxy for different metals grown on *i*-Al-Pd-Mn [42,43]. In contrast, our LEED patterns (Figs. 1, 4, S2, S5, and the video files) show that all the spots move toward the (0,0) spot with increasing beam energy. Importantly, no extra spots appear or splitting of the spots occur over the whole beam energy range. We also do not observe any signature of spots arranged in a periodic fashion that is characteristic of crystalline or approximant phases.

We, however, note that the thicker layers have disorder, as also corroborated by the theoretical clathrate model that is discussed later, which results in relative weakening of the LEED spots at larger thickness. But, what is very important is that all the LEED patterns show only quasiperiodic spots with no hint of any alternative ordering.

#### D. Quasicrystal clathrate model of Sn

The motifs observed from scanning tunneling microscopy as well as the low-energy electron diffraction patterns show structural signatures for the Sn film that are distinct from the substrate. Sn thus exhibits intrinsic quasiperiodic growth to a thickness of 3–4 nm, which is almost in the realm of bulk-like quasiperiodic growth where impact of the substrate becomes negligible. This is because the effective potential of a solid

including the exchange interaction term perpendicular to the surface is almost zero beyond unity Fermi wavelength [44]. Al and Mn that form the top layer of *i*-Al-Pd-Mn both have Fermi wavelengths of about 0.36 nm, which is almost an order of magnitude less than the 4-nm thickness of the quasiperiodic Sn layer. The function of the substrate is to suppress initial formation of stable crystalline forms of Sn, i.e., the  $\alpha$ - and  $\beta$ -Sn.

In Secs. III D through III I, we combine the geometrical concepts and DFT calculations, while in Sec. III J, we discuss how Sn white flower (SnWF) cluster facilitates nucleation of the intrinsic Sn structure. We show that the intrinsic Sn structure is a metastable clathrate quasicrystal and that in a narrow window of covering widths of 3–4 nm, an unsupported pentagonal clathrate structure is more stable compared to  $\alpha$ -Sn. In the  $\alpha$ -Sn structure, atoms are tetrahedrally coordinated and satisfy the  $sp^3$ -type bonding scheme. But there exists a whole family of alternative structures—*clathrates*—satisfying the same tetrahedral bonding scheme (Fig. 5), achieving that goal by grouping atoms around point centers into empty “cages.” Indeed, “empty” clathrates are experimentally achievable metastable states of Ge [45] or Si [46], and there is a broad family of clathrate structures that are stabilized by addition of large “host” atoms captured inside the cages. The clathrate structures are modular in the sense that the constituting polyhedral cages can be nontrivially recomposed into variety of periodic arrangements.

Two of the known clathrate structures commonly designated as types II and III exhibit a special relationship, illustrated in Figs. 6(a) and 6(b)—they share a common pseudo-five-fold axis, and equal vertical periodic repeat that is about 12.7 Å in the case of Sn. Size of the circles representing the atoms scales with their vertical height, and the neighboring atoms are connected by black lines along 2.9 Å-long interatomic bonds. Associating the centers of the decagonal rings



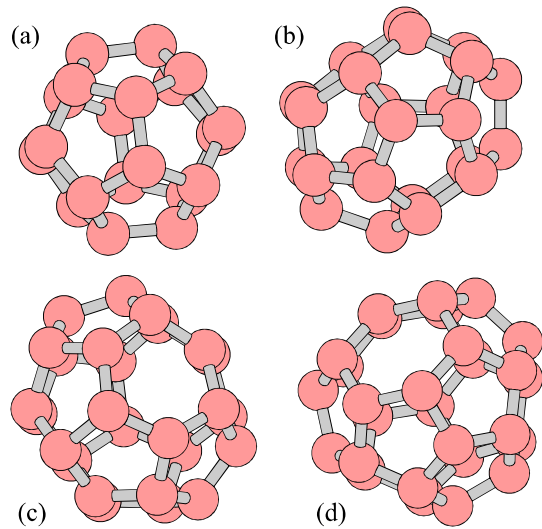


FIG. 5. The four different types of clathrate cages: (a) The smallest cage is a dodecahedron with coordination (CN) of 20. It is bounded exclusively by pentagonal faces and has full icosahedral symmetry. The bigger cages are bounded by either pentagonal or hexagonal facets with (b) CN = 24, (c) CN = 26, and (d) the largest with CN = 28.

(decorated inside by pentagons) with the tiling vertices reveals the geometric backbone of the structures: tiling of isosceles triangles  $T$  with wider angle  $72^\circ$  (two yellow and the longer blue sides) and rectangles  $R$  with aspect ratio  $\sqrt{\tau+2}/\tau$ ; blue linkages denoted  $b$  are about  $12.6 \text{ \AA}$  long, and the shorter yellow linkage  $y$  is given by  $b\tau/\sqrt{\tau+2} \sim 10.82 \text{ \AA}$ . Since the

tile decoration is symmetric and identical for all the yellow edges in both structures, and the same holds for the blue linkages. The cage motifs from two prototype structures can be combined to form a family of variant structures that are in one-to-one correspondence with planar rectangle-triangle (R-T) tilings. The R-T tilings may be arranged periodically as in Fig. 6(c), but the local fivefold axial symmetry of the cages eventually leads to global pentagonal order of the quasiperiodic structures [47]. Thus, the clathrate recipe for R-T tiling decoration gives rise to whole family of pentagonal structures, periodic, quasiperiodic, or disordered.

We note that the cage-cage linkage length in Sn clathrates of  $\approx 12.6 \text{ \AA}$  almost exactly coincides (to within 1%) with the pseudo-Mackay cluster-cluster separations in  $i\text{-Al-Pd-Mn}$  of  $12.55 \text{ \AA}$  ( $\tau$  times the intercluster linkages of  $7.7 \text{ \AA}$  between “mini-Bergman” or between “pseudo-Mackay icosahedra” clusters). In the clathrates, the prevalent dodecahedral cages have icosahedral symmetry, and sections through the cage normal to a fivefold axis will have pentagonal symmetry. Since the symmetry of the LEED patterns [Figs. 4 and S5] is determined by the surface layer, we predict that in general their symmetry will be fivefold.

#### E. Quasicrystal clathrates as duals of the Frank-Kasper structures

In Frank-Kasper (FK) structures, the space is divided into face-sharing tetrahedra. Decorating each tetrahedron center by Sn atom, every tetrahedron's face is intersected by a bond between pair of neighboring Sn atoms. Since there are four faces for every tetrahedron, every Sn atom is guaranteed to have four neighbors in the directions of the surrounding face centers. Thus, tetrahedrally close-packed structures

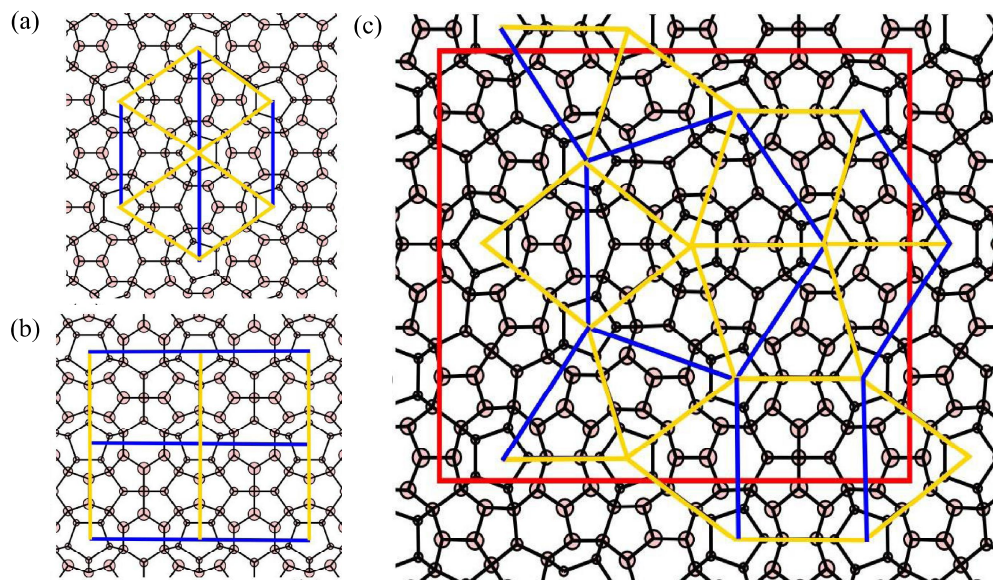


FIG. 6. The  $6 \text{ \AA}$ -thick sections through atomic structures of three clathrate approximants: (a) 136-atom cubic structure type II viewed along (110) direction; (b) 40-atom type III hexagonal structure viewed along (100) direction, and (c) 392-atom orthorhombic clathrate serving as ansatz for the decagonal clathrate. All the structures are shown along their common pseudodecagonal axis. The decagonal (in projection) rings can be associated with the vertices of tiling of rectangle-triangle (R-T) tiling. Case (a) is pure triangle tiling; case (b) is pure rectangles. Models are constructed by dual transformation of Frank-Kasper structures:  $\text{Cu}_2\text{Mg}$  (a),  $\text{Al}_3\text{Zr}_4$  (b), and hypothetical 22-atom orthorhombic decagonal approximant (c). The blue linkages are  $12.6 \text{ \AA}$  long.



TABLE I. Bulk DFT energies ( $dE$ , in meV/atom) of the Sn clathrates, relative to  $\alpha$ -Sn.cF8. First two rows are the basic clathrate types corresponding to decorated isosceles triangle tiles [type II, shown in Fig. 6(a)] and rectangles [type III, Fig. 6(b)]. Decagonal approximant (third row) combines cage motifs from type II and III structures following rectangle-triangle tiling geometry [Fig. 6(c)]. Last row reports 1/1 icosahedral approximant. Second and third columns show prototype and Pearson symbol of a dual FK structure, respectively, while fourth to seventh columns show the fraction of each kind of cage in the respective structure (Fig. 5), which are duals to the FK coordination polyhedra Z12–Z16.  $N_{at}$  reports the number of atoms per periodic cell.

Type	FK prototype	Name	C20	C24	C26	C28	$N_{at}$	$dE$
II	$\text{Cu}_2\text{Mg.cF24}$	Sn.cF136	0.666			0.333	34 <sup>a</sup>	28
III	$\text{Al}_3\text{Zr}_4.\text{hP7}$	Sn.hP40	0.429	0.286	0.286		40	40
Decagonal	$\text{Mg}_{28}\text{Zn}_{41}.\text{oP69}^b$	Sn.oP392	0.594	0.087	0.087	0.232	392 <sup>a</sup>	34
Icosahedral	$\text{AlMgZn.cI162}^c$	Sn.cI1840	0.593	0.259	0.074	0.074	920 <sup>a</sup>	48

<sup>a</sup>Calculation in primitive cell.

<sup>b</sup>Hypothetical structure.

<sup>c</sup>In the actual intermetallic structure of AlMgZn, two atoms—centers of Bergman clusters—are vacant.

are in one-to-one correspondence with their dual, clathrate relatives [48–50]. Four canonical FK polyhedra with triangulated coordination shells—Z12, Z14, Z15, and Z16—become respectively 20-, 24-, 26-, and 28-vertex cages, whose faces are pentagons and hexagons. This dual relationship is an alternative path to the decagonal clathrates defined above, by dual-transforming decagonal FK structures. The two clathrates from Figs. 6(a) and 6(b) are in fact dual relatives of the FK prototypes  $\text{Cu}_2\text{Mg}$  and  $\text{Al}_3\text{Zr}_4$  FK structures. Moreover, we could generalize clathrates to include 12-fold dodecagonal quasicrystals based on FK decoration of square-triangle tilings [51], whose strictly quasiperiodic version would be based on Stampfli’s square-triangle inflation rule [52].

The possibility of icosahedral FK structure whose dual would be perfect icosahedral clathrate is not clear. The only locally icosahedral and strictly tetrahedrally close-packed structure known is, to our knowledge, the “1/1” icosahedral approximant with prototypical natural realization in Al-Mg-Zn system, discovered by Bergman *et al.* [53]. In their milestone paper, Henley and Elser [54] described this structure as a simple decoration of Penrose rhombohedra and proposed that generalization of that decoration scheme eventually leads to FK quasicrystal enjoying global icosahedral symmetry. But there is a bottleneck: The decoration rule requires that all “oblate” rhombuses in the 3D Penrose tiling are paired along their short-body diagonals, but such tiling of 3D golden rhombuses is not known at present. An interesting aspect of the bulk icosahedral clathrate is its possible genuine entropic advantage over layered quasicrystals.

Relaxing the strict  $sp^3$ -bonding requirement (that translates into tetrahedral bonding rule) brings an interesting clue between spontaneously formed icosahedral quasicrystals in a model monoparticle system interacting via oscillating pair potentials [29] and real tin-based systems. As is clear from the phase diagram outlined in Fig. 3 of Ref. [29], the “low-density” icosahedral phase neighbors with clathrates, and major coordination number of that structure is four, although coordinations up to seven may occur. Given that Sn character is intermediate between  $sp^3$ -bonding type and metallic, which is reflected by the close competition of  $\alpha$  and  $\beta$  tin variants, such “imperfect” quasicrystal ordering seems entirely plausible.

### F. Cohesive energies and diffraction patterns of bulk Sn-clathrate models

While intermetallic clathrates are usually stabilized by 15% content of large guest atom that fits into large clathrate cages (and do not fit inside  $\alpha$ -Sn structure), even empty clathrate structures are energetically competitive. Fully relaxed cohesive DFT energies of these structures relative to the  $\alpha$ -Sn structure ground state are shown in Table I. The smallness of these energy differences (28–48 meV/atom range) as well as the fact that the decagonal approximant energy is intermediate between energies of type II and III prototype clathrates, are the first argument supporting the plausibility of the clathrate structure for Sn. We expect that the leading term in energetics of any clathrate structure will depend on the fraction of each type of the cage in the structure. Since the decagonal clathrate approximant (row 3 in Table I) cage fractions are intermediate between the two basic approximants (rows 1 and 2), its intermediate energy supports our expectation. On the other hand, the fact that the icosahedral approximant (row 4 in Table I) has highest energy, despite the fact that it is also structurally intermediate, suggests that the effective Hamiltonian should also tackle some pairwise cage-cage terms that did not occur in the 392-atom 2D approximant. Nevertheless, we would expect that the optimal bulk quasicrystal energy should lie in between 28- and 40-meV bounds provided by the extremes of fractional cage contents in the two basic type II and III clathrate approximants, but most likely very close to the energy of the decagonal approximant.

Figures 7(a) and 7(b) show that diffraction patterns of decagonal Sn-clathrate and the bulk  $i$ -Al-Pd-Mn phases parallel to their common fivefold axis exhibit striking similarity in both positions and intensity of the strong diffraction peaks. The apparent symmetry of the diffraction pattern is 10-fold in both cases, due to the presence of inversion symmetry in  $i$ -Al-Pd-Mn, and 10-fold screw axis in  $d$ -clathrate. The similarity of the patterns supports the Sn clathrate structural hypothesis.

### G. Energetics of unsupported Sn slabs

We further test the clathrate structural hypothesis by comparing the cohesive energies of the unsupported Sn slabs. We constructed reference series of the slabs of  $\alpha$ -Sn with the

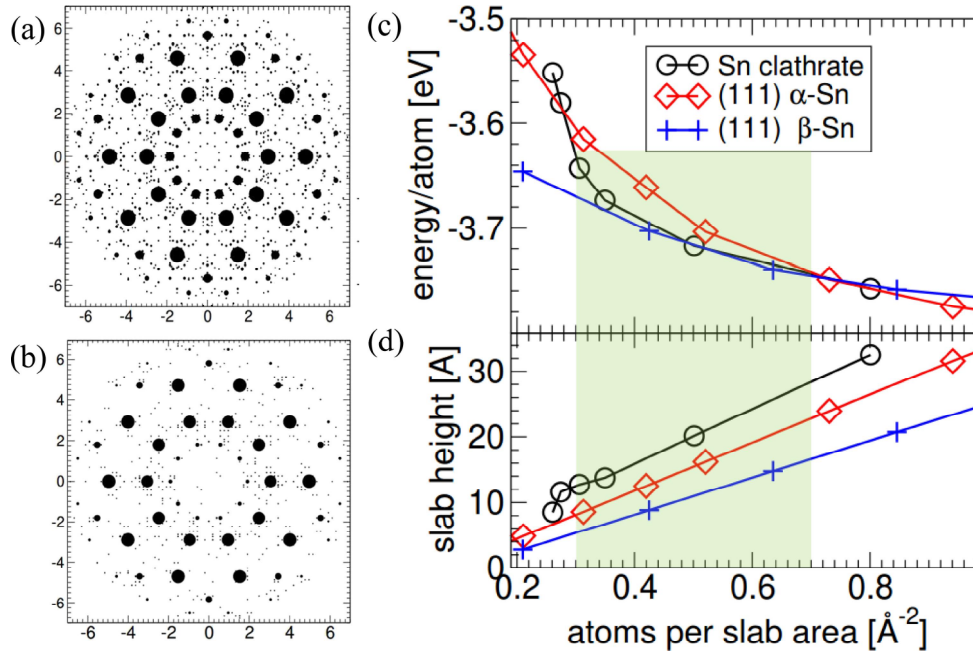


FIG. 7. The calculated diffraction patterns of the (a) large 2692-atom decagonal clathrate approximant and (b) *i*-Al-Pd-Mn represented by its “5/3” approximant. (c) Energy and (d) slab height as a function of the number of Sn atoms per slab area for  $\alpha$ -Sn,  $\beta$ -Sn, and the decagonal clathrate showing that in the 0.3–0.7 atom/ $\text{\AA}^2$  range (shaded light green), the clathrate is stable *wrt*  $\alpha$ -Sn. The increased height of the clathrate vs  $\alpha$ -Sn is due to higher density of the latter and large fluctuation of height on completed surface of the clathrate.

surface normal to (111) direction and of  $\beta$ -Sn with the surface normal to (100). These surfaces are flat planes in both cases and in  $\alpha$ -Sn atoms on the surface are threefold coordinated and in  $\beta$ -Sn fivefold coordinated (when we cut off the first coordination shell at about 3.3 Å).

For clathrates, we require that all the surface atoms have coordination equal to 3, like  $\alpha$ -Sn. This can be realized by growing the clathrate layer in discrete steps, by completing all (open) cages whose centers are nearest to the current surface. This strategy allows us to circumvent the difficulty of growing the “sparse” clathrate structure that does not contain well-defined flat layers, but rather coalesces sharing pentagonal/hexagonal faces between the neighboring cages.

In decagonal clathrates, the cage centers are located on four heights per 12.7 Å vertical repeat: Dodecahedra decorate the R-T tiling vertices at fractional height coordinates  $z = 0$  and  $0.5$ . The midedge and tile-interiors cage centers are all located at  $z = 0.25$  and  $z = 0.75$ . From this, we derived the aforementioned strategy for the slab construction: The surfaces are formed by completing all cages with next higher fractional coordinate  $z$ .

To represent the slab of the decagonal clathrate, we chose periodic approximant from Fig. 6(c). Slabs for all three structures,  $\alpha$ ,  $\beta$ , and decagonal clathrate approximant were fully optimized by relaxing ionic positions and lattice parameters until the average DFT force was less than 0.05 eV/Å, followed by single final self-consistent iteration with fixed geometry.

Energetics of sufficiently thick layers are characterized by bulk and surface energies,  $E_{\text{surf}} = (N \times E_{\text{bulk}} - E_{\text{lay}})/A/2$ ,

where  $E_{\text{bulk}}$  is bulk energy per Sn atom,  $E_{\text{lay}}$  is energy of the layer consisting of  $N$  atoms per periodic box, and  $A$  is the surface area. The bulk energy of the clathrate Sn approximant is stable compared to that of  $\beta$ -Sn by 11 meV/atom. In contrast, the former is unstable against  $\alpha$ -Sn by 35 meV/atom.

The surface energies, on the other hand, show the opposite trend, reaching a minimum for  $\beta$ -Sn slabs, with  $E_{\text{surf}} \sim 0.025$  meV/ $\text{\AA}^2$ , followed closely by clathrate (0.27 meV/ $\text{\AA}^2$ ), and  $\alpha$ -Sn (0.41 meV/ $\text{\AA}^2$ ). This result is consistent with  $\alpha$  and  $\beta$  surface energies calculated in Ref. [55], leading to prediction that sufficiently small Sn nanoparticles will consist of  $\beta$ -Sn even in the low-temperature limit (although that work does not include the possibility of nanoparticles based on clathrate cages).

In order to capture energetic competition between the three families of slabs, we evaluate and plot DFT energies of the slabs as a function of the number of atoms per unit area normal to the slab surfaces. The results are shown in Fig. 7(c), which plots cohesive energy/atom as a function of the area coverage. Figure 7(d) shows the height defined as a difference of the topmost and bottom atom coordinates ( $z_{\text{max}} - z_{\text{min}}$ ).

For thinnest slabs with coverages up to about 0.4 atom/ $\text{\AA}^2$ , the most stable structure is  $\beta$ -Sn. The clathrate approximant performs excellently for layer thickness exceeding approximately its one periodic repeat (about 12.7 Å), or twice the fivefold diameter of the fundamental dodecahedral cage: in the 0.3–0.7 atom/ $\text{\AA}^2$  covering range, i.e., for slab heights between 10 and 35 Å, it is more stable than  $\alpha$ -Sn [the range is shaded in light green in Figs. 7(c) and 7(d)]. It approximately equals energy of  $\beta$ -Sn in the range 0.5–0.7 atom/ $\text{\AA}^2$

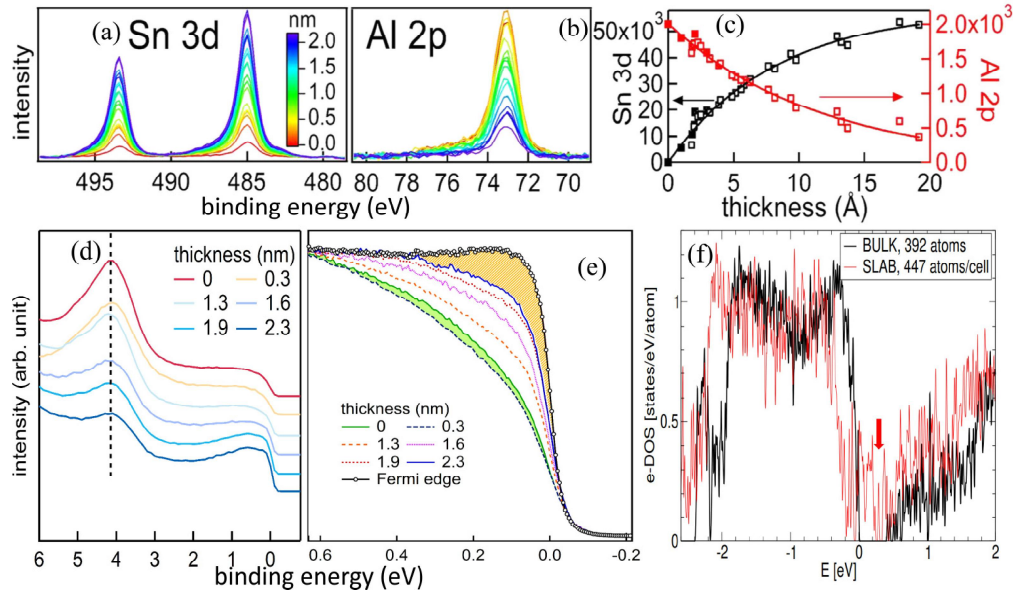


FIG. 8. (a) Sn 3d and (b) Al 2p XPS core-level spectra as a function of coverage and (c) the areas of the core-level peaks at 100 K (open squares) and RT (filled squares). The continuous lines are the least square fitted curves. (d) The valence band photoemission spectra of Sn/*i*-Al-Pd-Mn using UPS for different Sn coverages; the spectra are staggered along the vertical axis. (e) The UPS spectral shape close to the Fermi level ( $E_F$ ) for Sn layers up to thickness of 2.3 nm deposited at 150 K along with the Fermi edge of Mo foil in electrical contact with the specimen. The shaded orange region shows the suppression of intensity of the thick layer wrt the Fermi edge, confirming the existence of pseudogap. The shaded green region shows the deepening of the pseudogap compared to *i*-Al-Pd-Mn. (f) The calculated electronic density of states (DOS) of the 14 Å-thick relaxed Sn clathrate slab and its bulk parent structure. The bulk structure is repeated with 12.6 Å period, while the slab implementation contains about 14 Å-thick layer separated from its periodic image along the surface normal by about 33 Å-thick vacuum gap.

or 2- to 3-nm slab thickness. Finally, when the coverage exceeds 0.7 atoms/Å<sup>2</sup> or slab thickness  $\geq 3$  nm, i.e., approaching the bulk limit, the most stable structure is  $\alpha$ -Sn.

#### H. Photoemission spectroscopy and density of states from the clathrate model

In Figs. 8(a) and 8(b), Sn 3d<sub>5/2</sub> and Al 2p XPS core level spectra that appear at 485 and 73.1 eV, respectively, show no change in their binding energies with Sn coverage. This is a significant observation because core-level binding energies are sensitive to the transfer of electronic charge from the adsorbate to the substrate, which obviously can be ruled out in this case. The absence of core level shift or change in the shape also excludes the possibility of any alloying or intermixing of Sn with the substrate. This observation also implies a propensity for condensed island growth [18] as also shown in Fig. 2(a), indicating the dominance of adsorbate-adsorbate interaction. The Sn 3d<sub>5/2</sub> core level binding energy (485 eV) is similar to that of  $\alpha$ -Sn [56], indicating the similarity of the quasiperiodic Sn layer with that of  $\alpha$ -Sn, thus reaffirming the clathrate model where  $sp^3$  hybridization dominates. In Fig. 8(c), the intensity variation of the Sn 3d and Al 2p XPS core-level spectra exhibits an exponential trend as a function of thickness, indicating a layered growth, as also shown by STM. Figure 8(d) depicts the valence band of Sn/*i*-Al-Pd-Mn, where the prominent peak at 4-eV binding energy arises from Pd 4d-like states. It decreases in intensity with Sn deposition, but its binding energy remains unchanged, lending further

support to the conclusions drawn from the core-level spectra [Figs. 8(a) and 8(b)].

The stability of quasicrystals has been related to the existence of a pseudogap in the electronic DOS around the Fermi level ( $E_F$ ) originating from the interaction between the Fermi surface and the quasi-Brillouin zone of the quasicrystal [57–59]. In the valence band spectrum of *i*-Al-Pd-Mn [Fig. 8(d)], the pseudogap was ascribed to the rounded shape of the spectral function close to  $E_F$  [59]. With Sn deposition up to 1 ML (0.3 nm), we observe an interesting change in its shape [Fig. 8(e)]: The spectral weight decreases compared to *i*-Al-Pd-Mn, indicating a deepening of the pseudogap for the Sn monolayer, as is evident from the green shaded region. The pseudogap is observed up to the thickness of 2.3 nm (orange shaded region), as shown by the comparison with a metal Fermi edge in electrical contact with the specimen. However, for thicker layers, the pseudogap becomes shallower compared to the substrate, which is possibly related to the increase in disorder, as also shown by the relative weakening of the LEED spots, as discussed earlier in Sec. III C.

The DOS for relaxed bulk and slab Sn clathrate is shown in Fig. 8(f). It is interesting to note that the bulk Sn quasiperiodic clathrate is semiconducting with a band gap of about 0.4 eV, in contrast to bulk *i*-Al-Pd-Mn that shows a pseudogap [60]. In contrast to bulk, the DOS for the slab of Sn quasiperiodic clathrate shows a pronounced pseudogap with the minimum at 0.3 eV (red arrow), the states near  $E_F$  having almost equal contributions from the Sn *p* and Sn *d* states, while the contribution from the *s* states is marginal. The pseudogap is



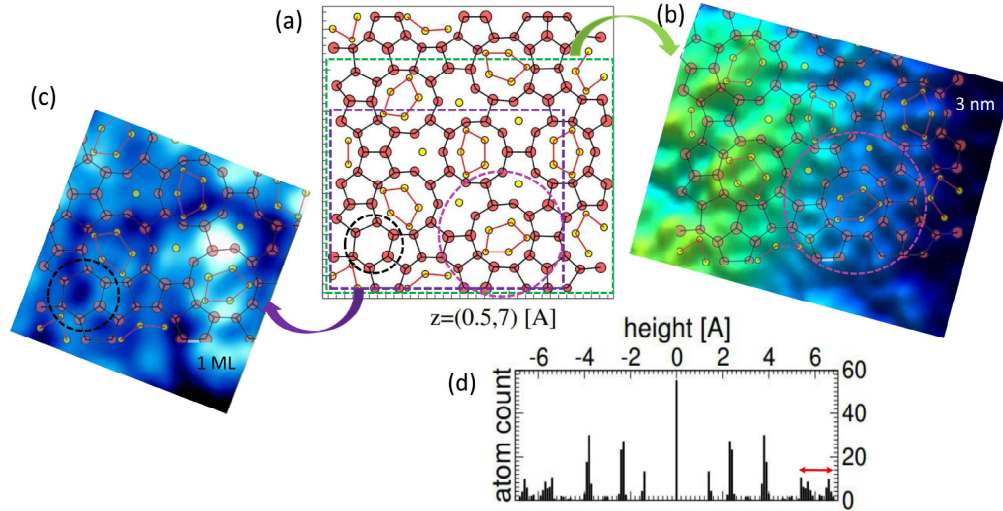


FIG. 9. (a) The most stable Sn clathrate slab fully optimized with surface relaxation using DFT for atom concentration of  $0.35 \text{ atom}/\text{\AA}^2$  with dimensions of  $35 \times 35 \text{ \AA}$ . (b) A part of the relaxed clathrate model enclosed by a green dashed rectangle in (a) is overlaid on the STM image of 3-nm-thick Sn layer [size  $16 \times 13 \text{ nm}$ , obtained from Fig. 3(d), that includes a crown motif highlighted by pink dashed circle] after  $\tau^3$  scaling (see text). (c) A part of the relaxed clathrate surface model enclosed by violet dashed rectangle in (a) is overlaid on the STM image of 1 ML Sn [size  $7 \times 7 \text{ nm}$ , obtained from Fig. 1(a), that includes a hexagonal tile centered motif highlighted by a black dashed circle]. (d) Height histogram of the Sn atoms within the slab; the red double arrow indicates the extent of puckering in the surface region.

deeper compared to *i*-Al-Pd-Mn, where the DOS was calculated for MS and M slabs [60]. Thus, the Sn clathrate model explains the interesting observation from photoemission that the pseudogap is deeper for the Sn monolayer compared to the substrate *i*-Al-Pd-Mn. It is worth noting that the interatomic bonding in Sn is different from Pb, where a wider pseudogap was reported from scanning tunneling spectroscopy, but it was later ascribed to the splitting of Pb  $6p$  band due to large spin-orbit coupling [19,24,25]. Pb does not have  $s$ - $p$  hybridization since the  $s$  and  $p$  bands are clearly separated, and thus the bonding is mediated by  $p$  orbitals only. Here, the deepening of the pseudogap around  $E_F$  results from formation of the puckered clathrate structure with high covalency and  $sp^3$  bonding between the Sn atoms. The clathrate structures perfectly support the  $sp^3$  bonding scheme, with exclusively tetrahedral local environments like in  $\alpha$ -Sn structure—but while in the latter the empty spaces are condensed into flat interlayer area, in clathrates they are isolated in four types of approximately spherical cages (Fig. 5).

### I. The relaxed clathrate model and the STM motifs

The structure of the most optimal surface of the Sn clathrate obtained by relaxing the atom positions in our DFT calculation is shown in Fig. 9(a). We find that it exhibits protruding dodecagons projecting down on the tiling vertex positions, while the pentagonal caps of the dodecahedral cages suffer considerable distortion. The height distribution of the Sn atoms shows existence of different layers in the slab [Fig. 9(d)]. However, their widths are considerable and in particular, the surface region shows that the spread in  $z$  is  $\approx 2 \text{ \AA}$  (red double arrow). This demonstrates that the surface is corrugated, in agreement with STM that shows large root-mean-square roughness (Sec. III C). Such large corrugation arises because the clathrate structure fills the

space very loosely and is made of large empty cages, and there may be wells even  $4 \text{ \AA}$  deep. Moreover, in reality, all the atom positions of the layer are not occupied and disorder is present, in agreement with the results from LEED discussed in Sec. III C.

The relaxed clathrate structure is in good agreement with STM and the motifs are also reproduced. For example, in Fig. 9(b), a part of the clathrate structure enclosed by green dashed rectangle is overlaid on a STM image from 3-nm-thick Sn layer that includes a crown motif (encircled by pink dashed circle) after  $\tau^3$  inflation and the agreement is found to be satisfying.  $\tau$  inflation is well known in quasicrystals due to their self-similar nature; for example, in *i*-Al-Pd-Mn, the fundamental intercluster linkage of  $7.75 \text{ \AA}$  is  $\tau$  inflated along the twofold direction, while  $\tau^3$  inflation is observed along fivefold or threefold directions.  $\tau^3$  inflation has also been reported in a binary quasicrystal Yb-Cd with the formation of cluster of clusters [61]. Figure 9(c) provides another example, where a STM image containing a hexagonal tile centered motif (encircled by black dashed circle) observed for 1 ML Sn is reproduced by a hexagon and the pentagons surrounding it from the violet dashed rectangle in Fig. 9(a) with  $\tau^2$  inflation. Thus, the relaxed clathrate model is able to reproduce the STM images [Figs. 9(b) and 9(c)], which reconfirms the validity of this structural model.

### J. Nucleation and compatibility of the Sn clathrate structure with *i*-Al-Pd-Mn

In this section, in order to find the genesis of the Sn clathrate structure and establish its compatibility with the substrate *i*-Al-Pd-Mn, we have studied the submonolayer coverages of Sn by STM to identify the nucleation centers. We find occurrence of pentagonal clusters that look like flowers with five bright petals at 0.2 ML coverage (encircled by orange

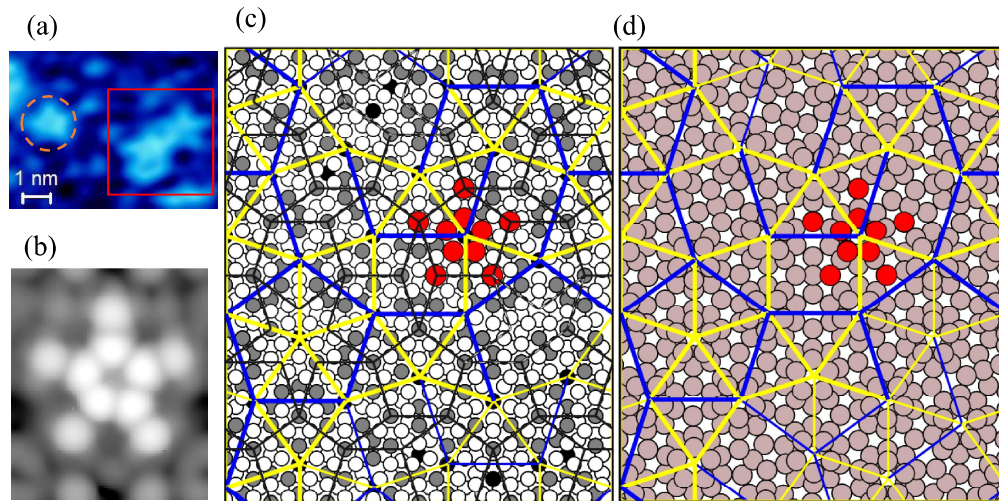


FIG. 10. (a) The STM image of Sn white flower (SnWF) for 0.2 ML Sn on *i*-Al-Pd-Mn with  $I_T = 0.6$  nA,  $U_T = 1.8$  V. (b) The calculated STM image of the SnWF cluster. The dimensions of the area are  $20.3 \times 23.9$  Å. (c) The known atomic structure of the 5/3 approximant of *i*-Al-Pd-Mn surface (Al, open circles; Pd, gray circles; Mn, black circles) with dimensions of  $53.2 \times 62.5$  Å. Red circles show the atomic configuration of the SnWF (starfish) cluster. (d) The atomic structure of the quasiperiodic Sn clathrate corresponding to the 5/3 approximant. The configuration of the starfish cluster (red) is a part of the clathrate structure.

dashes in Fig. 10(a); a larger area image is shown in Fig. S8 [35]). These clusters are formed on specific areas of the fivefold surface recognized in STM images as white flowers [63], and so we call them as the Sn white flower (SnWF) clusters. As shown in Fig. S8 by orange circles, the SnWFs are oriented in the same direction and are mostly isolated. However, we are able to identify regions, for example, inside the red rectangle in Fig. 10(a) that has two SnWFs that are nearest neighbors.

Similar fivefold clusters have also been observed for Pb [21] and Bi [20], which on the *i*-Al-Pd-Mn surface exhibit pseudomorphic growth up to a monolayer. In both systems, these fivefold clusters have been dubbed as the *starfish* clusters. On the *i*-Al-Pd-Mn surface, deposited Sn forms a thick layer with the structure of quasicrystalline clathrate. The SnWF clusters appearing at the submonolayer coverage play here an important role of nucleation centers for growth of the quasicrystalline layer.

To explain the role of the SnWF clusters, we use the model of the 5/3 approximant of *i*-Al-Pd-Mn [60,62]. The structure of the fivefold surface that can be described by the Penrose P1 tiling with an edge length of  $7.76$  Å [60] [black lines in Fig. 10(c)]. The tiling consists of pentagon, thin rhombus, star, and boat. The bulk structure of *i*-Al-Pd-Mn can be interpreted in terms of the pseudo-Mackay (pMC) clusters. On the fivefold surface, the pentagonal tiles represent sections over these pMC clusters. The equatorial section of the pMC cluster has a Mn atom in the center of the pentagonal tile [Fig. 10(c)] and in the STM image this motif is seen as the white flower mentioned above [63]. If the center of the pMC is deeper below the surface plane, this part of the surface corresponds to another characteristic pattern known as the *dark star* [63]. In the STM image of the bare surface shown in Fig. S1(c) [35], motifs of the white flower and the dark star can be well recognized.

At the submonolayer coverage, the SnWF cluster formed on the white flowers consists of 10 adatoms [24], as shown by the red atoms in Fig. 10(c). The calculated STM image of the SnWF is shown in Fig. 10(b), where shape is similar to that observed in the experiment [Figs. 10(a) and S8]. The central pentagon around this would show up as bright maxima in the STM images.

To examine the compatibility of the SnWF with the clathrate structure, it is interesting to compare the configuration of 10 Sn adatoms forming the SnWF cluster [Fig. 10(c)] (marked in red) with the structure of the clathrate layer [Fig. 10(d)]. The clathrate structure consists of regular dodecahedral cages of Sn atoms. The dodecahedra are centered at the vertices of the R-T tiling [Fig. 10(d)]. The top (or bottom) pentagonal face of the dodecahedron corresponds to the inner pentagon of the SnWF cluster.

The edges of the R-T tiling have two different lengths, the shorter  $y$  (yellow) and longer  $b$  (blue). In the *i*-Al-Pd-Mn structure, the length  $b = 12.55$  Å corresponds to the distance between two pMC clusters along the twofold directions. In the clathrate layer, each of the two neighboring dodecahedral cages at the distance of the longer edge  $b$  are connected over one Sn atom. This atom corresponds to the Sn atom from the outer pentagonal ring of the SnWF cluster. The bonding topology of the SnWF cluster is thus closely related to the structure of the Sn-clathrate and is a valid part of the clathrate structure. The SnWFs can thus serve as nucleation centers for growth of the quasiperiodic Sn adlayer with the clathrate structure.

On the other side, as the bulk structure of clathrate is different from the bulk structure of *i*-Al-Pd-Mn, there are also significant differences between the SnWF configurations on the *i*-Al-Pd-Mn surface and in the clathrate adlayer. On the fivefold Al-Pd-Mn surface, the SnWF cluster has essentially a planar structure and the interatomic bonding has a metallic



character. All the SnWF clusters on the surface have only one pentagonal orientation. In the atomic structure of the clathrate, the inner and outer pentagons of the SnWF clusters are at different heights. The interatomic bonding has the covalent  $sp^3$  character. They have both pentagonal orientations. The compatibility of the interface between the *i*-Al-Pd-Mn surface and the clathrate adlayer helps to stabilize the clathrate structure and prevents its conversion to a more stable crystalline structure.

Comparing Figs. 10(c) and 10(d), one can see that the arrangement of the tiles in a large part of the tilings on both models marked by thick blue and yellow lines are exactly the same. The parts of the R-T tilings on the *i*-Al-Pd-Mn and Sn clathrate surfaces with different arrangement of the tiles are marked by thinner lines. The reason why both tilings are not the same on the whole surface areas of the  $5/3$  approximants is the following: Out of four tiles of the P1 tiling describing ordering of atoms on the *i*-Al-Pd-Mn surface, three of them (pentagon, thin rhombus, and star) are compatible with the R-T tiling, but the boat tile contradicts the R-T ordering. On the  $5/3$  approximant model of the *i*-Al-Pd-Mn surface, there are two boat tiles [dashed black lines in Fig. 10(c)]. Around the boat tiles, the ordering of *i*-Al-Pd-Mn atoms can be again described by the R-T tiling (thin blue and yellow lines), however, with somewhat different arrangement of the tiles than in the clathrate model [Fig. 10(d)]. The boat tiles can thus induce defects in the R-T tiling. The presence of the boat tiles can be the origin of the observed partial disorder in the Sn adlayer.

#### IV. CONCLUSIONS

Our work demonstrates formation of a quasicrystalline structure in a thick Sn layer up to a thickness of at least 4 nm. Based on multiple pieces of evidence from both experiment and theory, we propose a quasiperiodic clathrate structural model for the Sn layer. Sn retains quasicrystallinity up to a thickness that is highest reported so far for any element, and this is almost in the realm of bulk-like growth, where the influence of the substrate potential is negligible. The STM motifs (crown, wheel, and hexagonal tile centered motif in Fig. 1) and the LEED IV curves (Fig. S3 of SM [35]) of the Sn monolayer are different from *i*-Al-Pd-Mn that is described by the Penrose P1 tiling. The motifs of the thick Sn layer are similar to the motifs of the first layer. This shows a structural difference between the Sn layer and the substrate, indicating that Sn grows with its intrinsic quasiperiodic structure and the substrate is unable to force a pseudomorphic growth. The role

of the substrate is solely to suppress initial formation of any stable crystalline forms of Sn.

Photoemission spectroscopy shows that the pseudogap around the Fermi level is deeper for the first Sn monolayer compared to *i*-Al-Pd-Mn and exists for the thick layer, indicating its stability. Using density functional theory, a comparative study of the free slab energies shows that surface energy favors clathrate over  $\alpha$ -tin up to about 4-nm layer thickness and matches  $\beta$ -tin for narrow window of slab thickness of 2–3 nm. The bulk clathrate exhibits a gap opening near Fermi energy, while the free slab form exhibits a pronounced pseudogap that explains the photoemission result. The STM images and the motifs observed on the Sn layer show good agreement with the proposed clathrate model. The SnWF clusters constitute the nucleation centers for growth of the quasiperiodic Sn adlayer since these are a valid part of the Sn clathrate structure. It is realized on the *i*-Al-Pd-Mn surface because the cluster-cluster separations (12.55 Å) observed on the latter enjoy magic consistency with the cage-cage separations in the Sn clathrate. Last but not the least, although here we do not observe Sn quasicrystal in the bulk form, the lower bulk total energy of the quasiperiodic Sn clathrate compared to  $\beta$ -Sn suggests that bulk quasicrystalline Sn might also exist in some part of its phase diagram.

#### ACKNOWLEDGMENTS

M.M. and M.K. are thankful for the support from the Slovak Grant Agency VEGA (No. 2/0082/17) and APVV (No. 15-0621). Parts of the calculations were performed in the Computing Center of the Slovak Academy of Sciences using the supercomputing infrastructure acquired under Projects ITMS 26230120002 and 26210120002. K.P. thanks CSC-IT Center for Science and the Academy of Finland under Grant No. 277829. Karsten Horn is thanked for his constructive suggestions and support. M. Maniraj is grateful to the C.S.I.R., New Delhi, for a research fellowship. J. Nayak, P. Bhakuni, and M. Balal are thanked for assistance during some of the experiments. Work by T.A.L. and D.L.S. was supported by the U.S. Department of Energy (DOE), Office of Science, Basic Energy Sciences, Materials Science and Engineering Division. The *i*-Al-Pd-Mn substrate was synthesized at the Materials Preparation Center, at the Ames Laboratory, which is operated for the U.S. DOE by Iowa State University under Contract No. DE-AC02-07CH11358.

V.K.S., M.M., M.K., S.S., P.S., M.M., and A.R. contributed equally to this work.

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